Molecular Dynamics simulations of lysozyme in water

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Objective: The main objective of this practical is to provide an overview of classical Molecular Dynamics (MD) simulations and Normal Mode Analysis (NMA) by examining the protein Lysozyme within the framework of the NAMD program.

1 Introduction

One of the principal tools in the theoretical study of biomolecules is the method of MD. It is a computational method which calculates the time dependent behaviour of a molecular system. MD methods are used to describe a complex molecular system in terms of a realistic atomic model, with an aim to understand and predict macroscopic properties based on detailed knowledge on an atomic scale.

MD simulations solve Newton’s equations of motion for a system of N interacting atoms:

\[ m_i \frac{\partial^2 r_i}{\partial t^2} = F_i, \quad i = 1, \ldots, N. \] (1)

The forces are the negative derivatives of the potential function \( V(r_1, r_2, r_3, \ldots, r_N) \):

\[ F_i = -\frac{\partial V}{\partial r_i}. \] (2)

The equations are solved simultaneously in small time steps. The system is followed for sometime, taking care that the temperature and pressure remain at the required values and the coordinates are written to an output file at regular intervals. The coordinates as a function of time represent a trajectory of the system. After initial changes, the system will usually
reach an equilibrium state. By averaging over an equilibrium trajectory many macroscopic properties can be extracted from an output file.

2 Potential energy function

Theoretical studies of biological molecules permit the study of the relationships between structure, function and dynamics at the atomic level. Since biological systems involve many atoms, quantum mechanical treatment of these atoms is not feasible. The usual way to solve them is to use empirical potential energy functions which are computationally less expensive, but involve numerous approximations leading to certain limitations. Current generation force fields provide a reasonable good compromise between accuracy and computational efficiency. They are often calibrated to experimental results and quantum mechanical calculations of small model compounds. Among the most commonly used potential energy functions are the AMBER, CHARMM, GROMOS and OPLS/AMBER force fields. One of the most important limitation of the empirical force fields is that no drastic changes in the electronic structure are allowed, i.e. no events like bond making or breaking can be modeled.

3 Setting up and running molecular dynamics simulations

To begin a molecular dynamics simulation, you must choose an initial configuration of the system, a starting point, or \( t = 0 \). Most often, in simulations of biomolecules, an X-ray crystal structure or an NMR structure is obtained from the Protein data bank (http://www.rcsb.org) and used as the initial structure. It is also possible to use a theoretical structure developed by homology modelling. The choice of the initial configuration must be done carefully as this can influence the quality of the simulation.

The MD simulations involves 4 main steps and these will be discussed below:

3.1 Energy minimization

The potential energy function of a biomolecular system is a very complex and multi-dimensional landscape. It has one deepest point, the global minimum and a very large number of local minima. The goal of the energy minimization is to find a local minimum. The energy at this local minimum may be much higher than the energy of the global minimum. Performing an energy minimization will guarantee the removal of any strong van der Waals interactions that may exist which might otherwise lead to local structural distortion and result in an unstable simulation.

3.2 Heating

The initial velocities at low temperature are assigned to each atom of the system and Newton's equations of motion are integrated to propagate the system in time. During the heating phase, initial velocities are assigned at a low temperature and the simulation is started with periodically assigning new velocities at a slightly higher temperature and letting the simulation continue. This step is repeated until the desired temperature is reached.
3.3 Equilibration

Once the heating process is over and the desired temperature is reached, the simulation is continued and during this phase, properties such as structure, pressure, temperature and the energy are monitored. The point of the equilibration phase is to run the simulation until these properties become stable with respect to time. If in the process, the temperature increases or decreases significantly, the velocities are scaled such that the temperature returns to its desired value.

3.4 Production and Analysis

The final step of the simulation is the production phase, wherein the system is simulated for the time length required from several hundred ps to ns or more. During this process coordinates of the system at different times are stored in the form of trajectories. These are then used for calculations of mean energy, root mean square (RMS) fluctuations between structures etc. From MD simulations, time dependent properties such as correlation functions can also be calculated and these in turn can be related to spectroscopic measurements.

4 Normal mode analysis

Normal Mode Analysis (NMA) is a classical technique for studying the vibrational and thermal properties of various molecular structures at the atomic level. Although this technique is widely used for molecular systems consisting of a small number of atoms, performing NMA on large-scale systems is computational challenging. Mathematically, the motion of the molecule is often described by a second order ordinary differential equation

\[ \ddot{q} + F_q = 0, \]  

where the matrix \( F_q \) is a force constant matrix derived from the second derivative of the potential with respect to the Cartesian coordinates. The standard procedure for solving this equation is to diagonalize the matrix \( F_q \) by computing its eigenvalues and eigenvectors. Each eigenvector is often referred to as a normal mode with certain vibrational frequency. The frequency is determined by the eigenvalue. The overall dynamics of the molecular system can be described by a superposition of a number of linearly independent normal modes.

5 Force field example: CHARMM

The force field description of the interatomic forces is split into two categories: the bonded terms and the non-bonded terms. The bonded terms regroup simple covalent binding as well as the more complex hybridization and \( \pi \)-orbital effects, these are the bonds, angles, dihedrals and improper-dihedrals terms. These terms are schematically drawn in Fig. 1. The non-bonded terms describe the van der Waals forces and the electrostatic interactions between the atoms. The different terms will now be presented in more detail.
Figure 1: Schematic representation of the bonded interaction terms contributing to the force field: bond stretching, angle bending, proper and improper dihedrals.

**Bond stretching**

The bond stretching term describes the forces acting between two covalently bonded atoms. The potential is assumed to be harmonic:

\[ V_b = k_b(b - b_0)^2 \]  

where \( b \) is the distance between the two atoms. Two parameters characterize each bonded interaction: \( b_0 \) the average distance between them and a force constant \( k_b \).

**Angle bending**

The angle bending terms describe the force originating from the deformation of the valence angles between three covalently bonded atoms. The angle bending term is described using a harmonic potential:

\[ V_\theta = k_\theta(\theta - \theta_0)^2 \]

where \( \theta \) is the angle between three atoms. There again two parameters characterize each angle in the system: the reference angle \( \theta_0 \) and a force constant \( k_\theta \).

**Torsional terms**

The torsional terms are weaker than the bond stretching and angle bending terms. They describe the barriers to rotations existing between four bonded atoms. There are two types of torsional terms: proper and improper dihedrals. Proper torsional potentials are described by a cosine function:

\[ V_\phi = k_\phi[1 + \cos(n\phi - \delta)], \quad n = 1, 2, 3, 4, 6 \]
where $\phi$ is the angle between the planes formed by the first and the last three of the four atoms. Three parameters characterize this interaction: $\delta$ sets the minimum energy angle, $k_\phi$ is a force constant and $n$ is the periodicity.

The improper dihedral term is designed both to maintain chirality about a tetrahedral heavy atom and to maintain planarity about certain atoms. The potential is described by a harmonic function:

$$V_\omega = k_\omega (\omega - \omega_0)^2$$  \hspace{1cm} (7)

where $\omega$ is the angle between the plane formed by the central atom and two peripheral atoms and the plane formed by the peripheral atoms (see Fig 1).

\textbf{van der Waals interactions}

Van der Waals interactions and electrostatic interactions are non-bonded interactions, i.e., they act between atoms which are not covalently bonded together.

The van der Waals force acts on atoms in close proximity. It is strongly repulsive at short range and weakly attractive at medium range. The interaction is described by a Lennard-Jones potential:

$$V_{vdW} = 4\epsilon \left[ \left( \frac{\sigma}{r} \right)^{12} - \left( \frac{\sigma}{r} \right)^6 \right]$$  \hspace{1cm} (8)

where $r$ is the distance between two atoms. It is parameterized by $\sigma$: the collision parameter (the separation for which the energy is zero) and $\epsilon$ the depth of the potential well. The Lennard-Jones potential is represented in Fig. 2.

\textbf{Electrostatic interactions}

Finally, the long distance electrostatic interaction between two atoms is described by Coulomb's law:

$$V_{Elec} = \frac{q_1 q_2}{4\pi \epsilon_0 r_{12}}$$  \hspace{1cm} (9)
where \( q_1 \) and \( q_2 \) are the charges of both atoms and \( r_{12} \) the distance between them. \( \epsilon_0 \) is the electric susceptibility of vacuum.

So finally, the equation for the potential energy describing the force field can be written:

\[
V = \sum_{\text{bonds}} k_B (b - b_0)^2 + \sum_{\text{angles}} k_\theta (\theta - \theta_0)^2 \\
+ \sum_{\text{proper dihedrals}} k_\phi [1 + \cos(m \phi - \delta)] + \sum_{\text{improper dihedrals}} k_\omega (\omega - \omega_0)^2 \\
+ \sum_{i,j} 4\epsilon_{ij} \left[ \left( \frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left( \frac{\sigma_{ij}}{r_{ij}} \right)^6 \right] + \sum_{i,j} \frac{q_i q_j}{4\pi \epsilon_0 r_{ij}}
\]  

(10)

### 5.1 Data Structures

The data structures include information about the molecule, its chemical composition, its chemical connectivity, certain atomic properties, internal coordinates for the energy function etc. This information for a particular class of molecule, e.g. protein and nucleic acids, is contained in the topology and parameter files.

#### 5.1.1 Residue topology file (RTF)

This file (top.chm) contains the information of the residues which are used to build large molecules. It contains the atom type, mass, hydrogen bond donors and acceptors as well as atoms partial charges in particular residue for each and every atom in the system.

#### 5.1.2 Parameter file (PARAM)

This file (par.chm) is associated with the RTF file as it contains all the necessary parameters for calculating the energy of the molecule. These include equilibrium bond distances, angles for bond stretching, angle bending and dihedral angle terms in the potential energy function as well as the force constants and the Leonard-Jones parameters.

#### 5.1.3 Protein structure file (PSF)

It is the most fundamental data structure for CHARMM. It is generated for a specific molecule and it is the concatenation of the information contained in the RTF file. It provides detailed information on the composition and the connectivity of the atoms in the molecule of interest. It gives the total number of bonds and provides information as to which atoms connect to form a particular bond. For all the bonds, angles, the torsion and the dihedral angles are listed. The PSF file must be specified before any calculation is performed. It contains the molecular topology, but not any information regarding bond lengths, angles etc. These informations are provided by the above topology and parameter files.

#### 5.1.4 Coordinate file (CRD)

The coordinate file contains the Cartesian coordinates of all atoms in the system. These are mostly obtained by the X-ray or the NMR experiments. Missing coordinates can be built
within CHARMM using the internal coordinate facility. In addition, the hydrogens which are not present in the X-ray crystal structure can also be built in by CHARMM by using the module HBUILD.

6  NAMD

NAMD is a parallel, Molecular Dynamics (MD) simulation program used to model biomolecular systems using high performance computing (HPC) clusters.

VMD is a molecular viewer program that can be used to help set up NAMD simulation and to help analyze and visualize NAMD output. VMD can be freely obtained from:


This tutorial provides a first introduction to NAMD and assumes that NAMD VERSION or later has been installed on your computer. For the accompanying VMD tutorial go to

http://www.ks.uiuc.edu/Training/Tutorials/

The tutorial is subdivided in two sections. The first one covers the basic steps of a MD simulation, i.e., preparation, minimization, and equilibration of your system. The second section introduces typical simulation techniques and the analysis of equilibrium properties.

For a detailed description of NAMD the reader is referred to the NAMD User’s guide located at

http://www.ks.uiuc.edu/Research/namd/current/ug/

The examples in the tutorial will focus on the study of lysozyme—a small protein with interesting properties.

In the next section, you will learn about typical NAMD input and output files and how to set up basic MD simulations. You will be generating output data by performing simulations and using other features of NAMD. These files are needed for the next sections. If you are not able to produce the output, correct versions have been provided for each section and may be found in the example-output folder inside the directory corresponding to the given simulation or exercise.

6.1  What is Needed

In order to run any MD simulation, NAMD requires (at least) the following:

- a Protein Data Bank (pdb) file which stores atomic coordinates and/or velocities for the system.\(^1\)

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\(^1\)Pdb files may be generated by hand, but they are also available via the Internet for many proteins at http://www.pdb.org.
a Protein Structure File (psf) which stores structural information of the protein, such as various types of bonding interactions.

- a force field parameter file. A force field is a mathematical expression of the potential which atoms in the system experience. The parameter file defines bond strengths, equilibrium lengths, etc.

- a configuration file, in which the user specifies all the options that NAMD should adopt in running a simulation. The configuration file tells NAMD how the simulation is to be run.

6.2 Lysozyme

As mentioned in the previous subsection, the first file needed to run an MD simulation with NAMD (in fact with any simulation package) is a pdb file. To do this, one needs to follow the next steps:

1. We first must download the protein structure file with which we will be working. For this tutorial, we will utilize hen egg white lysozyme (PDB code 1AKI). Go to the RCSB website and download the PDB text for the crystal structure (Figure 3).

2. Once you have downloaded the structure, you can visualize the structure using a viewing program such as VMD (Figure 4). Once you’ve had a look at the molecule, you are going to want to strip out the crystal waters. Note that such a procedure is not
universally appropriate (i.e., the case of a bound active site water molecule). For our intentions here, we do not need crystal water. There are (at least two ways) to do this:

(a) Use a plain text editor like vi, emacs, nedit (Linux/Mac), or Notepad (Windows). **Do not use word processing software!** Delete the lines corresponding to these molecules (residue "HOH" in the PDB file). Save the new .pdb with a new filename, e.g., 1AKI_noW.pdb.

(b) Alternatively, waters can be removed using VMD.

1. Launch VMD. Open VMD graphically by double-clicking on the VMD icon. Then, navigate to the NAMD-Tutorial/1.Build_system directory by using the cd command in the VMD command terminal:

   ```
   cd ~/NAMD-Tutorial/1.Build_system
   ```

2. Load 1AKI.pdb by clicking File → New Molecule menu item in the VMD Main window. In the Molecule File Browser use the Browse button to find the file 1AKI.pdb. Load it by pressing the Load button. Note that the X-ray structure from the Protein Data Bank does not contain the hydrogen atoms of lysozyme. This is because X-ray crystallography usually cannot resolve hydrogen atoms. The pdb file you will generate with psfgen along with the psf will contain guessed coordinates for hydrogen atoms of the structure. Later, energy minimization of the protein will ensure their positions are reasonable.

3. Choose the Extensions → Tk Console menu item and in the VMD TkCon window. Be sure you are in the ~/NAMD-Tutorial/1.Build_system directory. If you are not, navigate there using the Is command to list files and directories and the cd command to change directories. Then, type the following commands:

   ```
   set protein [atomselect top protein]
   Sprotein writepdb AKI_noW.pdb
   ```

   (Hit the Return key after each command.)

   In the previous step you have created the file AKI_noW.pdb, which contains the coordinates of the lysozyme alone without crystal waters, in the ~/NAMD-Tutorial/1.Build_system directory.

4. Quit VMD by choosing File → Quit.

3. Always check your .pdb file for entries listed under the comment MISSING, as these entries indicate either atoms or whole residues that are not present in the crystal structure. Terminal regions may be absent, and may not present a problem for dynamics. These missing atoms/residues must be modeled in using other software packages.

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2X-ray crystallography methods utilize the optical rule that electromagnetic radiation will interact most strongly with matter the dimensions of which are close to the wave-length of that radiation. X-rays are diffracted by the electron clouds in molecules, since both the wavelength of the X-rays and the diameter of the cloud are on the order of Angstroms. The diffraction patterns formed when a group of molecules is arranged in a regular, crystalline array, may be used to reconstruct a 3-D image of the molecule. Hydrogen atoms, however, are not typically detected by X-ray crystallography since their sizes are too small to interact with the radiation and since they contain only a single electron. The best X-ray crystallography resolutions currently available are around 0.9 Å.
6.3 Generating a Protein Structure File (PSF)

To prepare the psf file, you should follow the next steps:

1. Now, you will create the psf file of lysozyme. Note that VMD offers an automatic psf file builder via the VMD Main menu by clicking Extensions → Modeling → Automatic PSF Builder. We will create the psf file manually to teach you exactly how it is done. The psfgen package of VMD is very useful in this regard. In order to create a psf, you will first make a pgn file, which will be the target of psfgen. In a Terminal window type nedit to open the text editor. Type in the following lines:

   ```
   package require psfgen
topology top all27 prot lipid.inp
pdbalias residue HIS HSE
pdblalias atom ILE CD1 CD
segment A pdb 1AKI_noW.pdb
coordpdb 1AKI_noW.pdb U
guesscoord
writepdb lysozyme.pdb
writepsf lysozyme.psf
   ```

2. After typing this, save the file by clicking File → Save. Be sure that you are in the correct directory and enter the file name as 1AKI_noW.pgn. Quit the text editor by clicking File
→ Exit.
The file you just created contains the necessary commands to create the psf file of lysozyme with hydrogen atoms and without water. Each command of the pgn file is explained:

- Line 1: You will be running psfgen within VMD. This line requires that the psfgen package is available to be called by VMD.
- Line 2: Load the topology file top all27 prot lipid.inp
- Line 3: Change the residue name of histidine to the proper name found in the topology file. HSE is one of three names for histidine, based on the protonation state of its side group.³
- Line 4: The atom named "CD1" ($\delta$ carbon) in isoleucine residues is renamed as "CD", its proper name from the topology file. Since isoleucine contains only one $\delta$ carbon atom, the psf file does not use the number label after "CD".
- Line 5: A segment called A is created, containing all atoms from 1AKI_noW.pdb. The segment command also adds hydrogen atoms.
- Line 6: Coordinates are read from 1AKI_noW.pdb and residue and atom names are matched. Old segment labels will be overridden with the new segment label ?A?.
- Line 7: Coordinates of missing atoms (like hydrogens) are guessed based on residue definitions from the topology file.
- Line 8: A new pdb file with the complete coordinates of all atoms, including hydrogens, is written.
- Line 9: A psf file with the complete structural information of the protein is written.

3. In a Terminal window (again, be sure that you are in the ~/NAMD-Tutorial/1.Build_system directory), type the following command:

```
vmd -dispdev text -e 1AKI_noW.pgn
```

This will run the package psfgen on the file 1AKI_noW.pgn and generate the psf and the pdb file of lysozyme with hydrogens. In your screen you will see different messages. Warnings are related to the ends of your molecule and are normal.

4. Type exit in the Terminal to exit VMD. Two new files will appear in your working directory: lysozyme.pdb and lysozyme.psf. Check this by typing `ls` in a Terminal. You have created the psf!

³Histidine Residues. Of the 20 amino acids, histidine is the only one which ionizes within the physiological pH range (~7.4). This effect is characterized by the pKa of the amino acid side chain. For histidine, the value is 6.04. This leads to the possibility of different protonation states for histidine residues in a protein, and makes the consideration of the proper state important in MD simulations. The viable states are one in which the $\delta$ nitrogen of histidine is protonated (listed with residue name "HSD" in the topology file), one in which the $\epsilon$ nitrogen of histidine is protonated (?HSE?), and one in which both nitrogens are protonated ("HSP").
In this section we will learn how to solvate a protein, i.e., put inside water, to more closely resemble the cellular environment. You will do so by placing lysozyme in a water box, in preparation for minimization and equilibration with periodic boundary conditions.

1. In the VMD Main window, click Extensions → Tk Console. In the VMD TkCon window of your VMD session type:

```bash
package require solvate
solvate lysozyme.psf lysozyme.pdb -t 5 -o lysozyme_wb
```

The `package require solvate` command loads the `solvate package`, so that VMD will be able to call it.

The `solvate package` will put your protein in a box of water. The `-t` option creates the water box dimensions such that there is a layer of water 5 Å in each direction from the atom with the largest coordinate in that direction. The `-o` option creates the output files lysozyme_wb.pdb and lysozyme_wb.psf for lysozyme with the water box.

**Size of Water Box.** Ideally, one should work with a box which is large enough that the protein does not interact with its image in the next cell if periodic boundary conditions are used.
**Ions.** Ions should be placed in the water to represent a more typical biological environment. They are especially necessary if the protein being studied carries an excess charge. In that case, the number of ions should be chosen to make the system neutral. The ions present will shield the regions of the protein which carry the charge, and make the entire system more stable. They should be placed in regions of potential minima, since they will be forced to those regions during the simulation anyway. The psf file contains the charge of each atom and may be used to determine the charge of the total system or parts of it.

2. In the VMD Main window, click File → New Molecule. In the Molecule File Browser use the Browse button to find the file lysozyme_wb.psf. Load it by pressing the Load button. This will load the structural information into VMD.

3. In the same Molecule File Browser, browse for lysozyme_wb.pdb and load it. In the display, check if the water box surrounds lysozyme, and demonstrate to yourself that the hydrogen atoms now exist.

4. In the VMD TkCon window type:

   ```
   set everyone [atomselect top all]
   measure minmax $everyone
   ```

   This analyzes all atoms in the system and gives you the minimum and maximum values of x, y and z coordinates of the entire protein-water system. You will get something that looks like the following

   ```
   {4.311999797821045 -1.3930000066757202 -21.77199935913086}
   {52.625 50.944000244140625 22.663999557495117}
   ```

5. These values are defined relative to the origin of the coordinate system, set by the initial pdb file, 1AK1.pdb. The center of the water box may be determined by calculating the midpoint of each of the three sides in the coordinate system. Alternatively, one can use tcl scripting in VMD to find the center of the box by typing

   ```
   measure center $everyone
   ```

   in the VMD TkCon window. Determine the coordinates of the center of your water box and record these numbers. In our case:

   ```
   28.69862174987793 24.836271286010742 0.4592978060245514
   ```

6. Close VMD by choosing File → Quit in the VMD Main window.
Now that you have the pdb and psf files for solvated lysozyme, along with the parameter file for proteins in general, you only need a NAMD configuration file to be able to minimize and equilibrate your lysozyme-water system.
6.5 Analysis of the Structure and Parameter Files

This section of the practical uses files in your ~/Topology-Parameter directory and the files that you have generated just now (.pdb and .psf). The .psf file is the protein structure file. It contains information needed by NAMD to run the simulation. Each atom is associated with its mass, partial charge, atom reference number (in the topology file top.inp), and residue. Please ask your supervisor to explain these files, and the top.inp and par.inp files needed by NAMD in more detail.

1. How many amino acids and atoms are in lysozyme, how many atoms are hydrogen?
2. Which amino acids are in lysozyme, are they hydrophilic or hydrophobic?
3. How many CYS amino acids are present, what is their residue number and what is their respective distance (Cα-Cα in Å)?
4. How are the amino acids connected to each other? Name properties of this bond and explain their origin!
5. How many and which parameters are needed to describe the protein peptide bond (see par.inp)?

Di-Sulfide Bonds: Inspect the top.inp and par.inp files

6. What is the partial charge of the hydrogen (HS/HG1) and the sulfur (S/SG) atom in CYS?
7. What are the parameters for the sulfur-hydrogen (S-HS) and the sulfur-sulfur (SM-SM) bond? Which of these two bonds is stronger?

6.6 Minimization

In this section, you will examine the minimization of lysozyme in a water box with periodic boundary conditions.

**Periodic Boundary Conditions.** The use of periodic boundary conditions involves surrounding the system under study with identical virtual unit cells. The atoms in the surrounding virtual systems interact with atoms in the real system. These modeling conditions are effective in eliminating surface interaction of the water molecules and creating a more faithful representation of the in vivo environment than a water sphere surrounded by vacuum provides.

**Minimization and Equilibration.** Minimization and equilibration differ from each other by the nature in which they implement the molecular dynamics force field. Energy
minimization involves searching the energy landscape of the molecule for a local minimum, i.e., place in which the molecule is relaxed, by systematically varying the positions of atoms and calculating the energy. Energy minimization should remove any unwanted high-energy interactions that may have been present in the crystal structure. Equilibration involves molecular dynamics, whereby Newton Second Law is solved for each atom in the system to dictate its trajectory. Achievement of equilibrium is judged by how well velocities, pressure, etc. are distributed in the system over a given amount of time.

6.6.1 Configuration File

Go to your minimization directory by typing `cd 1.Minimization`. You will find a configuration file for the minimization of lysozyme in a water box. All output files for the minimization of your lysozyme in a water box system should be placed in this directory.

Open the configuration file, lysozyme.conf by typing `nedit lysozyme.conf`

- **Periodic Boundary Conditions**
  - Three periodic cell basis vectors are to be specified to give the periodic cell its shape and size. They are `cellBasisVector1`, `cellBasisVector2`, and `cellBasisVector3`.
  - `cellOrigin`: specifies the coordinates of the center of the periodic cell in Å. This is why you need to calculate the center of your water box after you solvate!
  - `wrapWater`: This command may be used with periodic boundary conditions. If a water molecule crosses the periodic boundary, leaving the cell, setting this command to on will translate its coordinates to the mirror point on the opposite side of the cell. Nothing can escape. The command may be set to on or off.
  - `wrapAll`: same as wrapWater, except this applies to all molecules.

- **PME (for full-system periodic electrostatics)**
  Particle Mesh Ewald or PME is a useful method for dealing with electrostatic interactions in the system when periodic boundary conditions are present. The Ewald sum is an efficient way of calculating long range forces in the periodic system. The particle mesh is a 3-D grid created in the system over which the system charge is distributed. From this charge, potentials and forces on atoms in the system are determined. As a result, your grid size should be chosen such that it is fine enough to accurately represent the configuration of your system.
  - `PME`: indicates whether or not the simulation uses the Particle Mesh Ewald Sum method; uses values yes and no.
  - `PMEGridSpacing`: sets the minimum ratio between the number of PME grid points along each `cellBasisVector` and the physical dimensions. Since the grid will replicate the charge distribution in your system, `PMEGridSpacing` should be chosen
to be large enough so that the grid spacing accurately reproduces your charge
distribution. However, it should not be so large that it will slow down your simu-
lation to provide unnecessary precision. Typically, a grid density of slightly more
than 1Å is a good choice to reproduce charge distribution in biological systems,
where the closest atoms have a bond separation on the order of 1 Å. This corre-
sponds to a PMEGridSpacing of 1.0. NAMD will then automatically set the PME
grid sizes (see below) such that there is always less than 1.0 Å between grid points
and the sizes contain only small prime factors (e.g. 2, 3, and 5). Alternatively, one
can define the PME grid sizes manually, using PMEGridSizeX, PMEGridSizeY, and
PMEGridSizeZ. These set the size of the PME grid along cellBasisVector1, 2 and 3,
respectively (not the x, y, and z directions as implied). For speed in computing
Fast Fourier Transforms, PMEGridSizeX should be chosen so that it can be factor-
ized by 2, 3, or 5. Note that since cellBasisVector is defined with slightly different
values in each direction, the size of the mesh spacing (in length) will be different
in each direction. Also, note also that when using the PME method, the com-
mand cutoff dictates the separation between long and short range forces for the
method; it does not simply turn off interactions.

• Output

– xstFreq: The extended system trajectory file contains a record of the periodic cell
parameters, essentially recording the trajectory of the cell boundaries over the
run time. This command specifies how often, in time steps, the configuration
will be recorded. If this command is set, three xst files will be output: 1 final and
2 restarts.

6.6.2 Run the minimization

Run your simulation by typing in a Terminal window:

```
  namd2 lysozyme_wb_eq.conf > lysozyme_wb_eq.log &
```

After minimization, energy are presented in the log file. The first lines confirm that
NAMD is writing the proper information at the proper time step, which you have specified
in the configuration file. The following space is where pressures would normally be written.
Note that since they are not pressures here, this space is used to store the total time step of
the simulation. Energies at that time step are then fully reported. In this case, they are output
every 100 time steps, as specified in the configuration file.

Follow the output as NAMD runs by typing `tail -f output.out`. At the end of the run,
type:

```
  grep 'ENERGY>' output.out > output.dat
```
to look at how the energy has changed during the simulation. This can be plotted using
XMGRACE. The second column will be the number of time steps (dimensionless), the third
the total energy (in kcal.mol\(^{-1}\)), and the fourth \(\Delta E\) (in kcal.mol\(^{-1}\)).
1. Plot the total energy vs. minimization step! Has the minimization converged?

If the energy hasn’t converged, create a new input file and edit it to increase the number of minimization steps. Run this new script with a similar command as above; output file will be `emin2.out` and the result of the `grep` command will be `emin2.dat`.

2. Examine the `.pdb` files before and after energy minimization using VMD. Notice any differences? (Hint 1: calculate the RMSD using VMD, Hint 2: first load the `.psf` and then the `.pdb` file into VMD.)

3. What is the greatest gradient during any of the minimizations? When does it appear and why?

4. Try to imagine a few structures for which the CHARMM force-field would give an energy that tends to \( \infty \).

6.7 Heating

- **Constant Pressure Control (variable volume)**
  - `useGroupPressure`: NAMD calculates system pressure based on the forces between atoms and their kinetic energies. This command specifies whether interactions involving hydrogen should be counted for all hydrogen atoms or simply between groups of hydrogen atoms; uses values yes and no and must be set to yes if rigidBonds are set.
  - `useFlexibleCell`: specifies whether or not you want to allow the three dimensions of the periodic cell to vary independently; uses values yes or no.
  - `useConstantArea`: NAMD allows you to keep the x ? y cross sectional area constant while varying the z dimension; uses values yes and no.
  - `langevinPiston`: indicates whether or not the simulation uses a Langevin piston to control the system pressure; uses values on and off.
  - `langevinPistonTarget`: specifies, in units of bar, the pressure which the Langevin piston tries to maintain. (1 atm = 1.013 bar)

- **Constant Temperature Control (variable volume)**
  The following are specifications for the Langevin piston which NAMD allows you to specify.
  - `langevinPistonPeriod`: sets the oscillation time constant in fs for the Langevin piston.
  - `langevinPistonDecay`: sets the damping time constant in fs for the Langevin piston.
  - `langevinPistonTemp`: sets the ?noise? temperature in K for the Langevin piston; should be set equal to the target temperature for the temperature control method (here, set by `langevinTemp`).
7 Analysis

This unit presents a series of examples of how to analyze data produced from NAMD simulations. For these examples you will not run the simulations themselves; instead you will analyze already produced data. Nevertheless, the instructions to set up and run the simulations are included, so you can actually produce the data yourself if time permits.

7.1 Equilibrium

This section contains exercises that will let you analyze properties of a system in equilibrium. The exercises mostly use pre-equilibrated trajectories from different ensembles to calculate properties of the lysozyme system.

7.1.1 Root Mean Square Deviation (RMSD)

1. Go to the directory 3.Analysis/a.rmsd/. You will use a script within VMD that will allow you to compute the average RMSD of each residue in your protein, and assign this value to the User field for each residue.

2. Load the structure file. First, open the Molecule File Browser from the File → New Molecule menu item. Browse for and Load the file lysozyme_wb.psf.

3. Browse for the file lysozyme_wb_eq.dcd located in the directory box/ and click on Load again. You can close the Molecule File Browser window.

4. Go to the TkCon window in VMD, and navigate to the 3.Analysis/a.rmsd/ directory.

5. The script you will use is called residue rmsd.tcl. In the TkCon window, type:

```source residue_rmsd.tcl```

This command itself does not actually perform any calculations. It reads the script residue rmsd.tcl which contains a procedure called rmsd residue over time. Calling this procedure will calculate the average RMSD for each residue you select over all the frames in a trajectory. The procedure is called as:

```rmsd_residue_over_time <mol> <sel_resid>```

where <mol> is the molecule in VMD that you select (if not specified, defaults to the top molecule), and <sel resid> is a list of the residue numbers in that selection.

6. For this example, you will select all the residues in the protein. The list of residue numbers can be obtained by typing in the TkCon window:

```set sel_resid [[atomselect top "protein and alpha"] get resid]```
The above command will get the residue numbers of all the α-carbons in the protein. The command will create a list of residue numbers in the variable $sel resid.

7. Call the procedure to calculate the RMSD values of all atoms in the newly created selection:

```
rmsd_residue_over_time top $sel_resid
```

You should see the molecule wiggle as each frame gets aligned to the initial structure. At the end of the calculation, you will get a list of the average RMSD per residue. This data is also printed to the file residue rmsd.dat. The procedure also sets the value of the User field of all the atoms of the residues in the selection to the computed RMSD value. You will now color the protein according to this value. You will be able to recognise which residues are free to move more and which ones move less during the equilibration. In order to use these new values to learn about the mobility of the residues, you will create a representation of the protein colored by User value.

8. Open the Representations window using the Graphics → Representations menu item.

9. In the Atom Selection window, type protein. Choose NewCartoon as Drawing Method, and in the Coloring Method drop-down menu, choose Trajectory > User. Now, in the Color Scale Data Range, type 0.40 and 1.00. Click the Set button. You should now see the protein colored according to average RMSD values. The residues displayed in blue are more mobile while the ones in red move less. This is somewhat counterintuitive, so you will change the color scale.

10. Choose the Graphics → Colors menu item. Choose the Color Scale tab. In the Method pull-down menu, choose for example GWB (Figure 7).

11. Plot the RMSD value per residue by typing in a Terminal window:

```
xmgrace residue_rmsd.dat
```

Take a look at the RMSD distribution (Figure 8). You can see regions where a set of residues shows less mobility. Compare with the structural feature of your protein. You will find a correlation between the location of these regions and secondary structure features like α helices or β sheets. When you are finished investigating the plot, close xmgrace, saving your plot if you wish.

### 7.1.2 Maxwell-Boltzmann Energy Distribution

| Objective: Confirm that the kinetic energy distribution of the atoms in a system corresponds to the Maxwell distribution for a given temperature. | 20 |
1. In a Terminal window, type `cd ../b.maxwell`. For this exercise, you need a file that contains the velocities of every atom for one instant of the simulation. You will use a file corresponding to the last frame of an equilibration of lysozyme. As discussed previously, one should use rigidBonds for water in any production simulation since water molecules have been parametrised as rigid molecules. But for the illustration of Maxwell-Boltzmann energy distribution, the effect of force field can be negligible. To be simple, we are not using the option rigidBonds. Here, we provide you with the file `lysozyme_wb_eq_.restart.vel`. Alternatively, you can use any velocity file, as long as constraints were not used in the simulation.

2. You will now load the structure file. First, open the Molecule File Browser from the File → New Molecule menu item. Browse for and Load the file `lysozyme_wb.psf`.

3. Now, browse for the file `lysozyme_wb_eq_.restart.vel` in the directory: `b.maxwell/Short_MD_without_rigidBonds`.

This time you need to select the type of file. In the Determine file type: pull-down menu, choose NAMD Binary Coordinates, and click on Load again. Close the Molecule File Browser. The molecule you loaded looks terrible! That is because VMD is reading the velocities as if they were coordinates. It does not matter how it looks, because what
we want is to make VMD write a useful file: one that contains the masses and velocities for every atom.

4. In the VMD TkCon window, navigate to the b.maxwell/ directory by typing `cd b.maxwell`.

5. First, you will create a selection with all the atoms in the system. Do this by typing in the TkCon window:

```
set all [atomselect top all]
```

6. Now, you will open a file energy.dat for writing:

```
set fil [open energy.dat w]
```

7. For each atom in the system, calculate the kinetic energy $\epsilon_k = \frac{1}{2} m v^2$, and 2 write it to a file

```
foreach m [all get mass] v [all get {x y z}] { puts $fil [expr 0.5 * $m * [vecdot $v $v] ] }
```

![RMSD Plot](image.png)

Figure 8: Plotting RMSD in xmgrace.
8. Close the file:

   close $fil

9. Outside VMD, take a look at your new energy.dat file. In a Terminal window, make sure you are in the 2-2-maxwell/ directory and type: nedit energy.dat It should look something like the list below (although the values will not necessarily be the same):

   1.26764386127
   0.189726622306
   0.268275447408
   ...

10. Quit nedit and VMD.

11. If you chose not to go through the steps above, there is a VMD script that reproduces them and will create the file energy.dat. In a Terminal Window, type:

   vmd -dispdev text -e get energy.tcl

   This will run VMD in text mode, source the script get energy.tcl, and produce the energy.dat file. When it is finished, type exit to exit VMD. You now have a file of raw data that you can use to fit the obtained energy distribution to the Maxwell-Boltzmann distribution. You can obtain the temperature of the distribution from that fit. In the rest of this section, we will show how to do this with the 2-D graphics package xmgrace. If you are more familiar with another tool, you may use it instead.

12. Quit VMD.

13. In a Terminal window, type xmgrace.

14. Once you see the xmgrace window, choose the Data \rightarrow Import \rightarrow ASCII menu item. In the Files box, select the file energy.dat. Click on the OK button. You should see a black trace. This is the raw data. You can now close the Read sets window.

15. To look at the distribution of points, you will make a histogram of this data. Choose the Data \rightarrow Transformations \rightarrow Histograms menu item. In the Source \rightarrow Set window, click on the first line, in order to make a histogram of the data you just loaded.

16. Click on the Normalize option.

17. Fill in Start: 0, Stop at: 10, and # of bins: 100. Click Apply.

18. You have created a plot, but you cannot see it yet. Use the right button of your mouse to click on the first set (in the Source \rightarrow Set window). Click on Hide. Now, go to the main Grace window and click on the button labeled AS, that will resize the plot to fit the existing values. This is your distribution of energies.
Now, you will fit a Maxwell-Boltzmann distribution to this plot and find out the temperature that the distribution corresponds to. (Hopefully, the temperature you wanted to have in your simulation!)

19. Choose the Data → Transformations → Non-linear curve fitting menu item. In the Source → Set window, click on the last line, which corresponds to the histogram you created.

20. In the Main tab, type in the Formula window:
\[ y = \frac{2}{\sqrt{\pi a_0^3}} * \sqrt{x} * \exp(-x/a_0) \]
This will fit the curve and get a fit for the parameter \(a_0\), which corresponds to \(k_B T\) in units of kcal/mol. (These are the energy units that NAMD uses)

21. In the Parameters drop-down menu, choose 1. Fill-in forms will appear below. You can give an initial value to \(A_0\), so that the iterations will look for a value in the vicinity of your initial guess. In the \(A_0\) window, type 0.6, which in kcal/mol corresponds to a temperature of \(~300\)K. The result are shown in Figure 9

![Figure 9: Maxwell-Boltzmann distribution for kinetic energies.](image)